



The network consists of three input layers and an intermediate layer. The three input layers – an eye-centered layer, an eye position layer and a head-centered layer – are also output layers; the final estimates of the network are read from these layers after relaxation. The three input layers consist of three topographic layers of  $N$  units indexed by their position,  $i$ (or  $j,k$ ), where  $i$ (or  $j,k$ ) =  $1 \dots N$ . Similarly, the intermediate layer is a topographic 2D map of  $N \times N$  units indexed by their position  $l, m$ , where  $l = 1 \dots N$  and  $m = 1 \dots N$ .

### 1. Connection weights

The input layers are symmetrically interconnected with the intermediate layer (hidden layer), and the corresponding matrices of connection weights are denoted by  $W^r$ ,  $W^e$ ,  $W^a$  for, respectively, the eye-centered, eye position and head-centered layers. The connection strengths between unit  $i$  ( $j,k$ ) in each input layer and unit  $(l,m)$  in the intermediate layer are given by

$$W_{ilm}^r = K_w \exp \left[ \frac{\cos[(2\pi/N)(i-l)] - 1}{\sigma_w^2} \right]$$

$$W_{jlm}^e = K_w \exp \left[ \frac{\cos[(2\pi/N)(j-l)] - 1}{\sigma_w^2} \right]$$

$$W_{klm}^a = K_w \exp \left[ \frac{\cos[(2\pi/N)(k-l-m)] - 1}{\sigma_w^2} \right]$$

The variable  $\sigma_w$  represents lateral spread: unit  $i$  is strongly connected if  $|i-l|/N \leq \sigma_w/2\pi$ . Note that with these connection matrices, unit  $(l,m)$  in the intermediate layer is most strongly interconnected with unit  $i=l$  in the eye-centered layer,  $j=m$  in the eye position layer and  $k=l+m$  in the head-centered layer. Unit  $(l,m)$  is connected more weakly to neighboring units in each layers, with the spatial extent of these connections is controlled by  $\sigma_w$ .

## 2. Network initialization

$R_{ri}(t)$ ,  $R_{ej}(t)$ , and  $R_{ak}(t)$  are denoted as the activity of unit  $i$  ( $j,k$ ) in the eye-centered, eye-position and head-centered layer at time  $t$ .

For eye-centered position, the probability distribution for the initial activity, denoted  $R_{ri}(0)$ , is given by

$$P(R_{ri}(0) | x_r) = \frac{f_i(x_r)^{R_{ri}(0)} \cdot e^{-f_i(x_r)}}{\Gamma(R_{ri}(0))},$$

$$f_i(x_r) = C_r \left( K \exp \left[ \frac{\cos[x_r - (2\pi/N)i] - 1}{\sigma^2} \right] + \nu \right)$$

The expressions for  $P(R_{ej}(0)|x_e)$  and  $P(R_{ak}(0)|x_a)$  are identical to  $P(R_{ri}(0)|x_r)$ , except that  $r$  is replaced by  $e$  or  $a$ . The expressions for  $f(x_a)$  and  $f(x_e)$  are identical to  $f_i(x_r)$  except that  $r$  is replaced by  $a$  or  $e$ .

The activity in the intermediate layer,  $A_{lm}(0)$ , is initialized to 0:  $A_{lm}(0) = 0$  for all  $l,m$ .

## 3. Recurrent network evolution

The evolution of the activities in the recurrent network is described by a set of coupled nonlinear equations. Denoting  $A_{lm}(t)$  as the activity of unit  $(l,m)$  in the intermediate layer at time  $t$ , the evolution equations are written

$$L_{lm}(t) = \sum_i W_{ilm}^r R_{ri}(t) + \sum_j W_{jlm}^e R_{ej}(t) + \sum_k W_{klm}^a R_{ak}(t)$$

$$A_{lm}(t+1) = \frac{L_{lm}(t)^2}{S + \mu \sum_l \sum_m L_{lm}(t)^2}$$

$$R_{ri}(t+1) = \frac{\left[ \sum_l \sum_m W_{ilm}^r A_{lm}(t+1) \right]^2}{S + \mu \sum_i \left[ \sum_l \sum_m W_{ilm}^r A_{lm}(t+1) \right]^2}$$

$$R_{ej}(t+1) = \frac{\left[ \sum_l \sum_m W_{jlm}^e A_{lm}(t+1) \right]^2}{S + \mu \sum_j \left[ \sum_l \sum_m W_{jlm}^e A_{lm}(t+1) \right]^2}$$

$$R_{ak}(t+1) = \frac{\left[ \sum_l \sum_m W_{klm}^a A_{lm}(t+1) \right]^2}{S + \mu \sum_k \left[ \sum_l \sum_m W_{klm}^a A_{lm}(t+1) \right]^2}$$

where  $L_{lm}(t)$  represents a linear pooling of activities from the three input layers. The activation functions  $A_{lm}$  or  $R_{ri}, R_{ej}, R_{ak}$  implement a quadratic nonlinearity coupled with a divisive normalization.

#### 4. Parameters used in the simulation

$K = 20$  Hz,  $\nu = 1$  Hz,  $\sigma = 0.40$  radians,  $K_w = 1$ ,  $\mu = 0.002$  s and  $S = 0.1$  Hz.  
 $\sigma_w = 0.37$  radians,  $C_r = C_e = C_a = 1$  s.